

Please check the examination details below before entering your candidate information

Candidate surname				Other names			
<b>Pearson Edexcel</b>		Centre Number			Candidate Number		
<b>Level 3 GCE</b>		<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>			<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>		
<b>Thursday 16 May 2019</b>							
Afternoon				Paper Reference <b>8FM0-24</b>			
<b>Further Mathematics</b> <b>Advanced Subsidiary</b> <b>Further Mathematics options</b> <b>24: Further Statistics 2</b> <b>(Part of option G only)</b>							
<b>You must have:</b> Mathematical Formulae and Statistical Tables (Green), calculator						Total Marks	

**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- The total mark for this part of the examination is 40. There are 4 questions.
- The marks for each question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1. Bara is investigating whether or not the two judges of a skating competition are in agreement. The two judges gave a score to each of the 8 skaters in the competition as shown in the table below.

	Skater							
	A	B	C	D	E	F	G	H
Judge 1	71	70	72	62	63	61	57	53
Judge 2	73	71	67	64	62	56	52	53

Bara decided to calculate Spearman's rank correlation coefficient for these data.

- (a) Calculate Spearman's rank correlation coefficient between the ranks of the two judges. (4)
- (b) Test, at the 1% level of significance, whether or not the two judges are in agreement. (4)

Judge 1 accidentally swapped the scores for skaters *D* and *E*. The score for skater *D* should be 63 and the score for skater *E* should be 62

- (c) Without carrying out any further calculations, explain how Spearman's rank correlation coefficient will change. Give a reason for your answer. (2)

a)

	A	B	C	D	E	F	G	H
Rank 1	2	3	1	5	4	6	7	8
Rank 2	1	2	3	4	5	6	8	7
<i>d</i>	1	1	-2	1	-1	0	-1	1
<i>d</i> <sup>2</sup>	1	1	4	1	1	0	1	1

$$\sum d^2 = 10$$

$$r_s = 1 - \frac{6\sum d^2}{n(n^2-1)}$$

$$= 1 - \frac{6(10)}{8(64-1)}$$

$$= 1 - \frac{60}{8(63)}$$

$$= \frac{37}{42}$$

$$\approx 0.881 \quad (3\text{sf})$$



Question 1 continued

$$b) H_0: \rho = 0$$

$$H_1: \rho > 0$$

critical value at 1% S.L. for  $n=8$  : 0.8333

$$r_s = 0.881 > 0.833 \quad (\text{lies within the critical region})$$

$\therefore$  Reject  $H_0$ . Evidence shows that the judges are in agreement.

c) The new ranks for D and E given by judge 1 is the same as judge 2 so  $\sum d^2$  will decrease so  $r_s$  will increase.

(Total for Question 1 is 10 marks)



2. Lloyd regularly takes a break from work to go to the local cafe. The amount of time Lloyd waits to be served, in minutes, is modelled by the continuous random variable  $T$ , having probability density function

$$f(t) = \begin{cases} \frac{t}{120} & 4 \leq t \leq 16 \\ 0 & \text{otherwise} \end{cases}$$

- (a) Show that the cumulative distribution function is given by

$$F(t) = \begin{cases} 0 & t < 4 \\ \frac{t^2}{240} - c & 4 \leq t \leq 16 \\ 1 & t > 16 \end{cases}$$

where the value of  $c$  is to be found.

(2)

- (b) Find the exact probability that the amount of time Lloyd waits to be served is between 5 and 10 minutes.

(2)

- (c) Find the median of  $T$ .

(2)

- (d) Find the value of  $k$  such that

$$P(T < k) = \frac{2}{3} P(T > k)$$

giving your answer to 3 significant figures.

a)  $\int \frac{t}{120} dt = \frac{t^2}{120(2)} + C$  (3)

$$= \frac{t^2}{240} + C$$

when  $t = 4$ ,  $\frac{t^2}{240} + c = 0$

$$\frac{4^2}{240} + c = 0$$

$$c = -\frac{1}{15}$$

$$\Rightarrow \frac{t^2}{240} - \frac{1}{15}$$



Question 2 continued

$$\begin{aligned}
 \text{b) } P(5 < T < 10) &= F(10) - F(5) \\
 &= \left( \frac{10^2}{240} - \frac{1}{15} \right) - \left( \frac{5^2}{240} - \frac{1}{15} \right) \\
 &= \frac{100 - 25}{240} \\
 &= \frac{5}{16}
 \end{aligned}$$

$$\text{c) } F(t) = 0.5$$

$$\begin{aligned}
 \frac{t^2}{240} - \frac{1}{15} &= \frac{1}{2} \\
 t^2 &= \left( \frac{1}{2} + \frac{1}{15} \right) 240 \\
 &= 136 \\
 t &= \sqrt{136} \\
 t &\approx 11.7
 \end{aligned}$$

$$\text{d) } P(T < k) = F(k)$$

$$P(T > k) = 1 - F(k)$$

$$F(k) = \frac{2}{3} \left( 1 - F(k) \right)$$

$$\frac{k^2}{240} - \frac{1}{15} = \frac{2}{3} \left[ 1 - \left( \frac{k^2}{240} - \frac{1}{15} \right) \right]$$

$$\frac{k^2}{240} - \frac{1}{15} = \frac{2}{3} \left( \frac{16}{15} - \frac{k^2}{240} \right)$$

$$\frac{k^2}{240} - \frac{1}{15} = \frac{32}{45} - \frac{k^2}{360}$$

$$\frac{k^2}{360} + \frac{k^2}{240} = \frac{32}{45} + \frac{1}{15}$$

$$\frac{k^2}{144} = \frac{7}{9}$$

$$k^2 = 144 \left( \frac{7}{9} \right)$$

$$k = \sqrt{112}$$

$$= 4\sqrt{7}$$

$$k \approx 10.6 \quad (3\text{sf})$$



**Question 2 continued**

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**Question 2 continued**

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**(Total for Question 2 is 9 marks)**

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3. Two students, Jim and Dora, collected data on the mean annual rainfall,  $w$  cm, and the annual yield of leeks,  $l$  tonnes per hectare, for 10 years.

Jim summarised the data as follows

$$S_{wl} = 42.786 \quad S_{ww} = 9936.9 \quad \sum l^2 = 26.2326 \quad \sum l = 16.06$$

- (a) Find the product moment correlation coefficient between  $l$  and  $w$  (2)

Dora decided to code the data first using  $s = w - 6$  and  $t = l - 20$

- (b) Write down the value of the product moment correlation coefficient between  $s$  and  $t$ .  
Give a justification for your answer. (1)

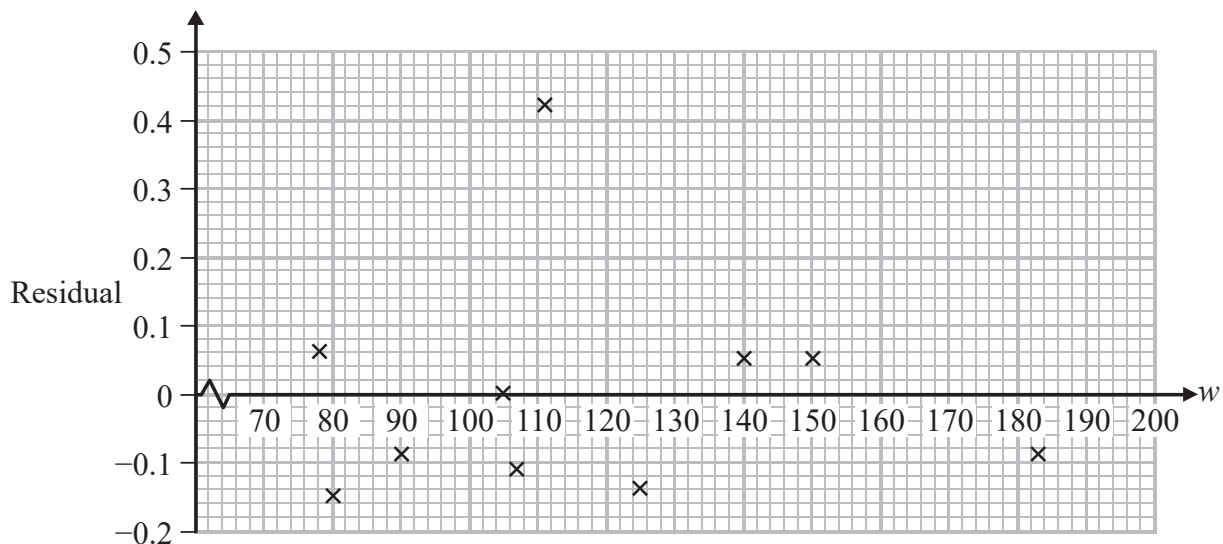
Dora calculates the equation of the regression line of  $t$  on  $s$  to be  $t = 0.00431s - 18.87$

- (c) Find the equation of the regression line of  $l$  on  $w$  in the form  $l = a + bw$ , giving the values of  $a$  and  $b$  to 3 significant figures. (3)

- (d) Use your equation to estimate the yield of leeks when  $w$  is 100 cm. (1)

- (e) Calculate the residual sum of squares. (2)

The graph shows the residual for each value of  $l$



- (f) (i) State whether this graph suggests that the use of a linear regression model is suitable for these data. Give a reason for your answer.  
(ii) Other than collecting more data, suggest how to improve the fit of the model in part (c) to the data. (2)





Question 3 continued

$$a) S_{ll} = \sum l^2 - \frac{(\sum l)^2}{n}$$

$$= 26.2326 - \frac{(16.06)^2}{10}$$

$$= 0.44024$$

$$r = \frac{S_{wl}}{\sqrt{S_{ww} \times S_{ll}}}$$

$$= \frac{42.786}{\sqrt{9936.9 \times 0.44024}}$$

$$= 0.64689$$

$$\approx 0.647 \quad (3sf)$$

b)  $0.647$ . ( $r$  is not affected by linear coding)

$$c) l - 20 = 0.00431(w - 6) - 18.87$$

$$l = 0.00431w + 1.10414$$

$$l = 0.00431w + 1.10$$

$$d) l = 0.00431(100) + 1.10$$

$$= 1.531$$

$$\approx 1.53$$

$$e) R_{ss} = S_{ll} - \frac{(S_{wl})^2}{S_{ww}}$$

$$= 0.44024 - \frac{(42.786)^2}{9936.9}$$

$$= 0.256 \quad (3sf)$$

fi) Residuals are randomly scattered around zero so linear regression model is suitable.

ii) The outlier can be removed and the regression line can be calculated



**Question 3 continued**

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4. The random variable  $X$  has a continuous uniform distribution over the interval  $[5, a]$ , where  $a$  is a constant.

$$\text{Given that } \text{Var}(X) = \frac{27}{4}$$

(a) show that  $a = 14$

(3)

The continuous random variable  $Y$  has probability density function

$$f(y) = \begin{cases} \frac{1}{20}(2y-3) & 2 \leq y \leq 6 \\ 0 & \text{otherwise} \end{cases}$$

The random variable  $T = 3(X^2 + X) + 2Y$

(b) Show that  $E(T) = \frac{9857}{30}$

(7)

$$\text{a) } \frac{1}{12} (a-5)^2 = \frac{27}{4}$$

$$(a-5)^2 = \frac{27}{4} (12)$$

$$= 81$$

$$a = \sqrt{81} + 5$$

$$= 14 \quad (\text{since } a > 5)$$

$$\text{b) } E(X) = \frac{5+14}{2}$$

$$= 9.5$$

$$\text{Var}(X) = E(X^2) - [E(X)]^2$$

$$\frac{27}{4} = E(X^2) - 9.5^2$$

$$E(X^2) = \frac{27}{4} + 9.5^2$$

$$= 97$$

$$E(Y) = \int_2^6 \frac{1}{20} y(2y-3) dy$$

$$= \int_2^6 \left( \frac{1}{10} y^2 - \frac{3}{20} y \right) dy$$

$$= \left[ \frac{y^3}{30} - \frac{3y^2}{40} \right]_2^6$$

$$= \left( \frac{36}{5} - \frac{27}{10} \right) - \left( \frac{8}{30} - \frac{3}{10} \right)$$

$$= \frac{68}{15}$$



Question 4 continued

$$\begin{aligned} E(T) &= E(3(X^2 + X) + 2Y) \\ &= 3[E(X^2) + E(X)] + 2E(Y) \\ &= 3(97 + 9.5) + 2\left(\frac{68}{15}\right) \\ &= \frac{9857}{30} \end{aligned}$$

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Question 4 continued

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**Question 4 continued**

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**(Total for Question 4 is 10 marks)**

**TOTAL FOR FURTHER STATISTICS 2 IS 40 MARKS**

**END**

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